

CO₂ Velocity Measurements and Models for Temperatures down to -10 °C and up to 200 °C and Pressures up to 100 MPa

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Summary

Studies concerning how CO₂ velocity is affected by a wide range of temperatures and pressures are important in understanding CO₂ behavior in fluid and rock systems. Three laboratory experiments were carried out to investigate the effect of temperature and pressure on CO₂ velocity for the range $-10\text{ }^{\circ}\text{C} \leq T \leq 200\text{ }^{\circ}\text{C}$ and $7\text{ MPa} \leq P \leq 100\text{ MPa}$. The results show that CO₂ velocity increases as pressure increases and as temperature decreases in the temperature ranges of $-10\text{ }^{\circ}\text{C} \leq T \leq 20\text{ }^{\circ}\text{C}$ and $25\text{ }^{\circ}\text{C} \leq T \leq 200\text{ }^{\circ}\text{C}$. Near the critical point (31°C and 7.4 MPa), CO₂ velocity is very sensitive to temperature and pressure change. CO₂ velocity models were developed to better match the experimental data.

Introduction

Recently, carbon dioxide has been considered as an important agent in global warming that has occurred due to rising temperature of the earth. The increased concentrations of CO₂ in the atmosphere have been associated with human activity. Extensive studies on the properties of CO₂ have been undertaken both experimentally and theoretically in order to find ways to minimize its impact on the environment. Consequently, CO₂ sequestration, injection and storage are increasingly becoming the climate change and industrial strategies of oil companies. In oil and reservoir conditions, temperature and pressure are higher up to 200 °C and 100 MPa. At lower temperature, one way to combat climate change is to store CO₂ in to the deep ocean around 3000 meters where temperature and pressure are about 6.9 °C and 40 MPa. Pipeline conditions are usually in the ranges of temperature -20 to 50°C and pressure 5 to 25 MPa (Folas et al., 2007). To understand the properties of CO₂ at a wide range of temperature and pressure is crucial for CO₂ operations. Theoretically, many equations of state are unable to predict the thermodynamic properties of CO₂ accurately over the entire range of temperature and pressure required for CO₂ operations (Batzle,1998). Laboratory measurements of acoustic properties of CO₂ are rarely available beyond 40 MPa.

In the Rock Physics Laboratory (RPL), University of Houston, the CO₂ velocity has been measured over a wide

range of temperature from $-10\text{ }^{\circ}\text{C}$ to 200°C and pressure from 7 MPa up to 100 MPa. Models were built to fit the measured data.

Experiments

Considering different behaviors of CO₂ velocity in the wide range of temperature and pressure, we separated the interested region to the three parts:

- the low temperature and high pressure range:
 $-10\text{ }^{\circ}\text{C} \leq T \leq 20\text{ }^{\circ}\text{C}$ and $20\text{ MPa} \leq P \leq 100\text{ MPa}$.
- the high temperature and high pressure range:
 $25\text{ }^{\circ}\text{C} \leq T \leq 200\text{ }^{\circ}\text{C}$ and $20\text{ MPa} \leq P \leq 100\text{ MPa}$.
- the low pressure range:
 $7\text{ MPa} < P < 20\text{ MPa}$.

Correspondently, three experiments were performed.

Measurement results and discussions

Since the CO₂ is a fluid in the measured range, we can use the following definition of the compressional velocity to understand its properties (McCain, 1990),

$$V_p = \sqrt{\frac{K}{\rho}}$$

where K is bulk moduli and ρ is density.

Velocity properties in the low temperature and high pressure range

The measured velocities within the low temperature and high pressure range $-10\text{ }^{\circ}\text{C} \leq T \leq 20\text{ }^{\circ}\text{C}$ and $20\text{ MPa} \leq P \leq 100\text{ MPa}$ are plotted in Fig.1. The compressional velocity increases as pressure increases at a given temperature, but it decreases as temperature increases at a given pressure. Because CO₂ is liquid below the critical temperature 31°C and above the critical pressure 7.4 MPa, the bulk modulus increases faster than density with increasing pressure. At a given pressure, increasing temperature will increase pressure. But in order to keep the constant pressure, releasing the pressure will decrease the bulk modulus faster than the density, and then the velocity decreases. The effects of the temperature and pressure become more pronounced as the pressure decreases to below 40 MPa, since the CO₂ liquid is approaching to the critical point and the phase boundary of liquid and gas.

CO₂ Velocity Measurements and Models

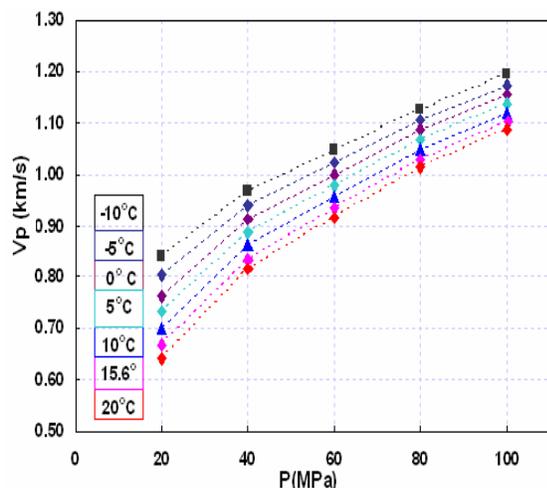


Fig.1 Measured velocities of CO₂ as a function of pressure P for different temperatures from 20 °C down to -10 °C.

Velocity properties in the high temperature and high pressure range

Like in the low temperature range, the CO₂ velocity increases as pressure increases at a given temperature, and it decreases as temperature increases at a given pressure (Fig.2). But the temperature effect becomes complicated. A small increase in temperature causes a large decrease in the velocity when temperature is lower. Higher temperature has less effect to decrease velocity than that of lower temperature. For example, when the pressure is around 40MPa, the temperature increases 25°C from 25°C to 50°C, the velocity decreases several times comparing to the temperature increases from 150°C to 200°C, where the velocity doesn't lower much by the temperature increases.

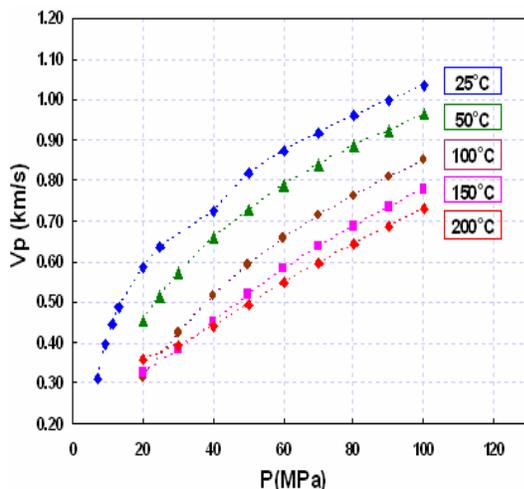


Fig.2 Measured velocities of CO₂ as a function of pressure P for different temperatures from 25 °C up to 200 °C.

With the temperature increases over the critical temperature (31°C), CO₂ is supercritical fluid. Because the properties of the supercritical fluid are more like “gas” at the low pressure range, the effects become greater as the pressure decreases to below 40 MPa. Generally, the compressional velocity in the CO₂ gas phase decreases as pressure increases because density increases faster than the bulk modulus. But in the supercritical fluid phase, the velocity also increases as pressure increases because the bulk modulus also increases fast with a given temperature. When the pressure increases over 20 MPa, the bulk modulus increase faster than the density, therefore, the velocity continues to increase with pressure increases.

Velocity properties around the CO₂ critical point

The velocity properties around the CO₂ critical point (31° C and 7.4 MPa) are very sensitive to temperature and pressure change. There are liquid phase, gas phase, liquid/gas phase boundary and supercritical fluid in the region. Even within the range of pressure up to 40 MPa, the temperature and pressure effects are still complicated. Fig. 3 shows the measured data around the critical point, the temperature from 25°C to 45°C and pressure from 7 MPa to 13 MPa.

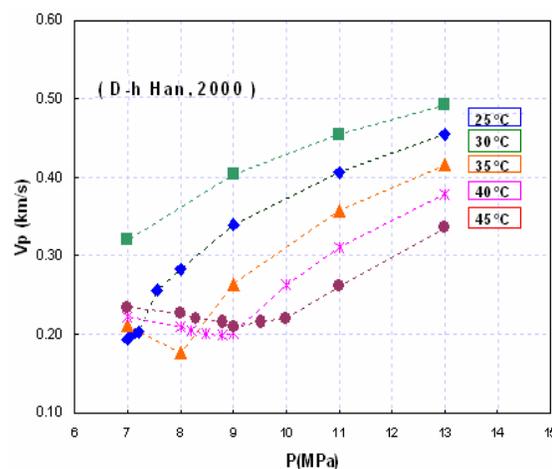


Fig.3 Measured velocities of CO₂ as a function of pressure P for the range near the CO₂ critical point.

With the pressure above the critical point from 7.4 to 13 MPa and the temperature bellows the critical point, the CO₂ is in the liquid phase. The velocity increases with pressure increases. Above the supercritical temperature (31° C), the CO₂ is the supercritical fluid. The velocity decreases to a certain point first, and then increases as the pressure increases. The turn point of the velocity shows the property of the supercritical fluid changed from like “gas” when the pressure is lower, to like “liquid” with pressure increases.

CO₂ Velocity Measurements and Models

Empirical Models

Empirical models have been developed to fit the experimental data and to describe the effects of temperature and pressure on CO₂ velocity.

Model for the low temperature and high pressure range

Based on the experimental result, the following polynomial model is suitable to describe CO₂ velocity as a function of temperature and pressure for this range,

$$V_p = a + bT + cT^2 + dP + eP^2 + fTP,$$

where

$$\begin{aligned} a &= 0.61571 & b &= -0.00709 & c &= 0.00002 \\ d &= 0.00833 & e &= -0.00003 & f &= 0.00004. \end{aligned}$$

The result of comparing the calculated CO₂ velocities with the measured data shown in Fig. 4, indicates that the model is correct to evaluate the CO₂ velocity at the range of temperature and pressure, $-10^\circ\text{C} \leq T \leq 20^\circ\text{C}$ and $20\text{ MPa} \leq P \leq 100\text{ MPa}$.

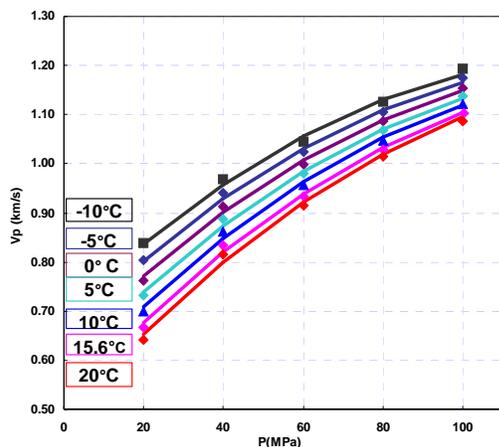


Fig.4 Calculated (solid lines) and measured velocities of CO₂ as a function of pressure P for different low temperatures from 20 °C down to -10 °C.

Model for the high temperature and high pressure range

The measured data show that the CO₂ velocities of the high temperature range are more likely extended from those of the low pressure area. We can use the following model to better match the measured data within the two regions, the high temperature and high pressure range, and the low pressure range,

$$V_p = (1 - W_f)V_{lp} + W_f V_{hp},$$

where

$$W_f = \frac{W_{f1} + |W_{f1}|}{2(0.5 + |W_{f1}|)}$$

$$V_{lp} = 150 + 120T_{pr} - [9 + 175(1.5 - T_{pr})^2]P_{pr}$$

$$V_{hp} = 45 + 600(a - T_{pr})^3 + 246|P_{pr} - S_{hp}|^{0.44}$$

$$W_{f1} = (P_{pr} + 7.661 - bT_{pr})^9$$

$$P_{pr} = \frac{P}{7.386} + 4.20831 \frac{T^{1.43}}{(c - T)(1 + 1.249 P)}$$

$$T_{pr} = \frac{1}{304.21} [T_{abs} - d(304.21 - T_{abs})]$$

$$T_{abs} = T + 273.15$$

The parameters for the high temperature and high pressure range are

$$a = 1.71 \quad b = 7.789 \quad c = 312 \quad d = 0.$$

In Fig.5, comparing the computed CO₂ velocity with the measured data shows that the model can be used to predicate CO₂ velocity at a wide range of temperatures (from 25°C to 200°C) and pressures (from 20 MPa to 100 MPa).

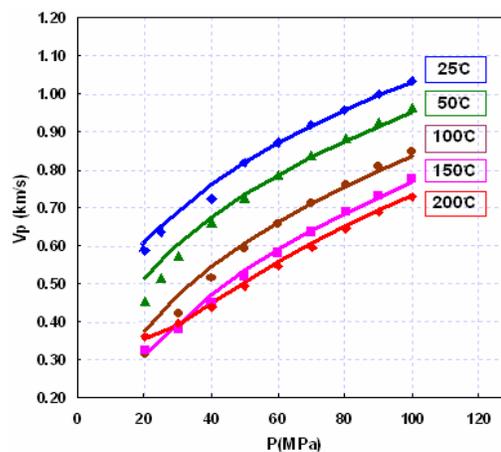


Fig.5 Calculated (solid lines) and measured velocities of CO₂ as a function of pressure P for different temperatures from 25 °C up to 200 °C.

Model for the low pressure range

Since the low pressure range from 7 to 20 MPa includes the CO₂ critical point, the velocity is very sensitive to temperature and pressure change. The model for the high temperature and high pressure range can be used to predict its behavior with the parameters,

$$a = 1.66 \quad b = 6.405 \quad c = 30000 \quad d = 40.$$

CO₂ Velocity Measurements and Models

The result shown in the Fig.6 indicates they are matched, but the more laboratory data are needed to correct the model, especially near the critical point.

Comparing the measured CO₂ velocities with calculated by the model and by Span & Wagner's equation of state (EOS)

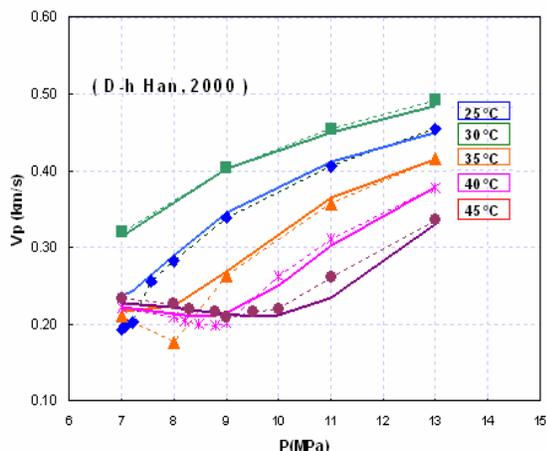


Fig.6 Calculated (solid lines) and Measured (dashed lines) velocities of CO₂ as a function of pressure P for the range near the CO₂ critical point.

(Span and Wagner, 1996) is shown in Fig.7 and Fig.8. The EOS equation for carbon dioxide is able to describe almost all reliable measured data within their experimental uncertainty, and is valid in the wider fluid region from the triple-point temperature to 1100K at pressures up to 800

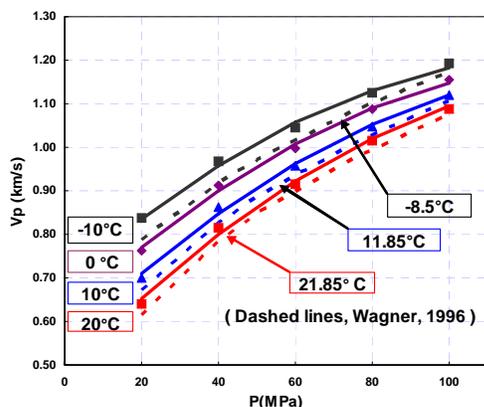


Fig.7 Comparing the calculated (solid lines) and measured velocities with the calculated velocities (dashed lines) by Span and Wagner for the low temperature and high pressure range.

MPa. The equation is accurate but contains many terms. Some of the terms are complex exponential which become difficult for computation. Our model with less terms and simple exponentials is simpler and easier to use. Fig.8 shows that the model is less accurate than Span and Wagner's in the lower pressure regions but more of a match to the measured data as pressure increases.

Conclusions

Laboratory experiments were carried out to study the effects of temperature and pressure on CO₂ velocity for a wide range of temperatures and pressures, $-10^{\circ}C \leq T \leq 200^{\circ}C$ and $7 MPa \leq P \leq 100 MPa$.

Clearly, CO₂ velocity increased as pressure increased and temperature decreased at the ranges of $-10^{\circ}C \leq T \leq 20^{\circ}C$, $20 MPa \leq P \leq 100 MPa$ and $25^{\circ}C \leq T \leq 200^{\circ}C$, $20 MPa \leq P \leq 100 MPa$. When pressure bellows to 20 MPa, CO₂ velocity is vary sensitive to temperature and pressure change. The CO₂ velocity models have been developed to match the experimental data and describe the relationships of CO₂ velocity with temperature and pressure. However, more laboratory data are needed to limit the bias of the experimental data and to correct the models.

Acknowledgments

This research has been supported by the "Fluids/DHI" consortium, which is sponsored by industry and collaborated between University of Houston and Colorado School of Mines.

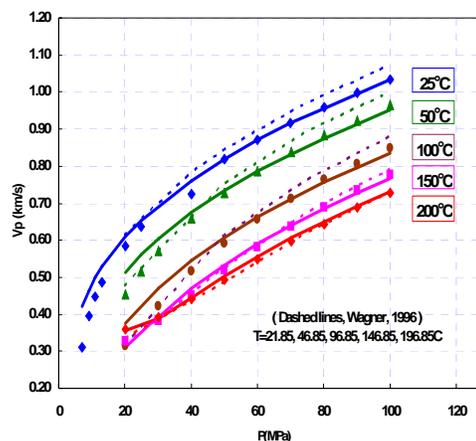


Fig.8 Comparing the calculated (solid lines) and measured velocities with the calculated velocities (dashed lines) by Span and Wagner for the high temperature and high pressure range.

EDITED REFERENCES

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